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CALCULATION OF THE SWEEP SPATIAL FABRIC SHELL TAKING INTO ACCOUNT THE FORMING PROPERTIES OF THE MATERIAL

Abstract: *The article is devoted to the design of textile spatial shells. The purpose of this work is to develop a method for designing parts of a woven shell of a spatial form, taking into account the molding properties of the material. As a result of theoretical studies, an analytical method has been developed for obtaining a sweep of a tissue membrane around a dome-shaped surface.*

Keywords: *The cloth; textile shell; Shell design.*

One of the methods for designing and manufacturing fabric volumetric casings is a method that takes into account the most important technological property of the mesh structure of fabric - the ability to take a volumetric shape by changing the angles between the warp and weft threads.

The quality of fabric products is largely determined by the validity of the developed design. One of the directions for intensifying and improving the quality of designing such products is the automation of the design processes of product parts. At the same time, the mathematical apparatus incorporated in the programs for calculating the sweep of the shells should provide high accuracy in determining the contours of the sweeps and a fairly accurate determination of the deformations of the tissue that occur during the formation of bulk surfaces.

The purpose of this work is to develop an analytical method for designing parts of a dome-shaped woven shell (a combination of areas of a sphere and a cone), taking into account the forming properties of the material.

To obtain a sweep above the specified shell, it is sufficient to consider the sweep of the $\frac{1}{4}$ part when the zero weft thread U_0 and the zero warp thread S_0 are perpendicular to each other (Fig. 1). On the surface, the fabric mesh forms the curvilinear coordinate system $SM_{00}U$. The web of the fabric forms cells with side dimensions $-l_x$ along the warp threads and $-l_y$ along the weft threads. The calculation of the sweep parameters can be significantly accelerated by increasing the size of the tissue cells, but an increase in the dimensions of the sides leads to unacceptable errors in the calculation of parameters [1.2].

The lengths of the warp and weft threads in the cell were determined by linear interpolation [3,4,5]. When the ratio $S/R \leq 0.4$, the error does not exceed 0.02 mm, which ensures the required sweep accuracy.

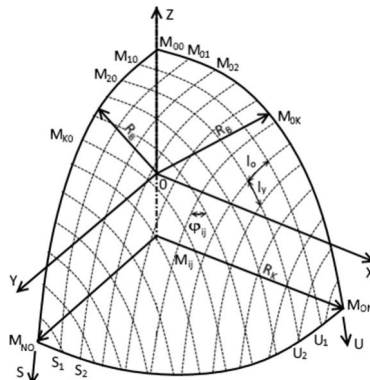


Fig. 1. Scheme of a tissue shell of a spatial form

Based on this, to determine the unfolding of the shell, a sufficient accuracy can be obtained by dividing the fabric mesh into cells with side dimensions $l \leq 40$ mm. Since the zero threads of the warp S_0 and weft U_0 lie on the perpendicularly directed meridians of the sphere, the coordinates of the nodal points of these threads M_{i0} and M_{0j} (Fig. 2) can be determined from the dependence

$$\begin{aligned} X_{i0} &= R_b \sin \alpha ; X_{0j} = 0 ; Y_{i0} = 0 ; Y_{0j} = R_b \sin \alpha ; Z_{i0} = R_b \cos \alpha ; Z_{0j} = R_b \cos \alpha \\ \text{where } i &= j = 0; 1; 2; \dots; k \end{aligned} \quad (1)$$

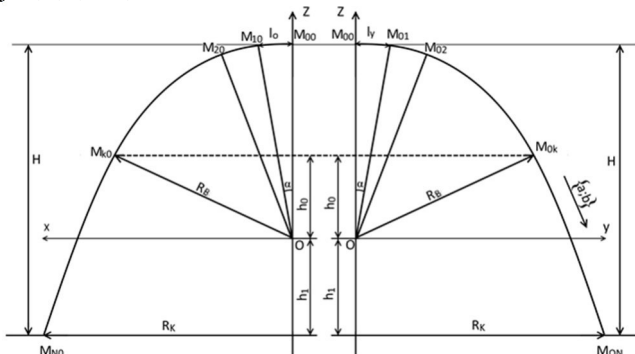


Fig. 2. Zero warp and weft threads on the shell surface

X_{i0} ; Y_{i0} ; Z_{i0} – coordinates of points M_{i0} , lying on the intersection of zero warp thread S_0 and j – th weft thread U_j , mm; X_{0j} ; Y_{0j} ; Z_{0j} – coordinates of points M_{0j} , lying at the intersection of the zero thread of the weft U_0 and the i – th warp thread S_i , mm; l_o and l_y — sizes of fabric cells, respectively, along the warp and weft threads, mm; R_b – radius of the sphere, mm; R_k – radius of the lower part of the cone,

mm; h_o , h_i , H - respectively the height of the tapered part and the entire product; α - is the radian measure of the arc, rad (Fig. 2).

To determine the coordinates of the nodal points on the zero warp and weft threads on the conical part of the surface, consider a unit vector that forms the cone. The coordinates of this vector will look like:

$$a = \frac{h_o}{R_b} \quad b = \frac{\sqrt{R_b^2 - h_o^2}}{R_b}$$

Then the coordinates of the nodal points on the surface will be determined from the dependencies:

$$X_{io} = \sqrt{R_b^2 - h_o^2} + a l(i - k); \quad Y_{io} = 0; \quad Z_{io} = h_o + b l(i - k)$$

$$X_{oj} = 0; \quad Y_{oj} = \sqrt{R_b^2 - h_o^2} + a l(j - k); \quad Z_{oj} = h_o + b l(j - k) \quad (2)$$

where $i=j=k+1; \dots, N$

N - is the number of points falling on the tapered part

Determination of the number of points falling on the spherical and conical part of the surface is carried out according to the formulas:

$$R_b \cos \alpha = h_o \Rightarrow k = \frac{(\arccos R_b \cos \frac{h_o}{R_b})}{\alpha} \quad N = \frac{|M_N M_K|}{1} \quad (3)$$

Next, it is necessary to determine the coordinate of the point - h_o along the Z axis, which determines the level of transition of the sphere into a cone.

According to $h_1 = H - R_b$ coordinates M_N и M_K can be depicted as follows:

$$M_N(-R_k; h_1); \quad M_K(\sqrt{R_b^2 - h_o^2}; h_o)$$

Based on the fact that $\overrightarrow{M_N M_k} \perp \overrightarrow{OM_k}$ we write

$$\frac{\sqrt{R_b^2 - h_o^2}}{h_o - h_1} = \frac{h_o}{\sqrt{R_b^2 - h_o^2}}$$

this implies $R_b^2 + h_o^2 + R_k \sqrt{R_b^2 - h_o^2} = h_o^2 - h_1 h_o$

$$R_k^2 R_b^2 - R_k^2 h_o^2 = R_k^4 - 2 R_b^2 h_1 h_o + h_1 h_o$$

$$h_o^2 (h_1^2 + R_k^2) - 2 R_b^2 h_1 h_o + R_b^2 (R_b^2 - R_k^2) = 0$$

Solving the square equation, we find

$$h_o = \frac{R_b^2 h_1 + \sqrt{R_b^4 h_1^2 + (h_1^2 + R_k^2)(R_k^2 - R_b^2) R_b^2}}{h_1^2 + R_k^2} = \frac{R_b^2 h_1 + R_b \sqrt{R_k^2 h_1^2 + R_k^4 - R_b^2 R_k^2}}{h_1^2 + R_k^2} \quad (4)$$

The next step is to calculate the coordinates M_{ij} of the point. To calculate these coordinates, consider a cell formed by the intersection of warp and weft threads on a spherical surface (Fig. 3a).

Using vector properties [6;7], knowing the coordinates of the anchor points $M_{00}; M_{01}; M_{10}$:

$$\vec{r}_{00} = \{X_{00}; Y_{00}; Z_{00}\} \quad \vec{r}_{11} = \{X_{10}; Y_{10}; Z_{10}\} \quad \vec{r}_{01} = \{X_{01}; Y_{01}; Z_{01}\}$$

find the coordinates of the point M_{11} :

$$\vec{r}_{11} = 2 \frac{\vec{r}_{01} + \vec{r}_{10}}{(\vec{r}_{01} + \vec{r}_{10})^2} \left(\vec{r}_{00} \left(\vec{r}_{01} + \vec{r}_{10} \right) \right) - \vec{r}_{00} = \frac{2\cos\alpha}{1-\cos r_{10}r_{01}} \left(\vec{r}_{01} + \vec{r}_{10} \right) - \vec{r}_{00} \quad (5)$$

Consider the case when the points go to the tapered part of the surface, since the cone is isometric to the plane, we write down the equation that describes the surface of the cone in a cylindrical coordinate system (Fig. 3b).

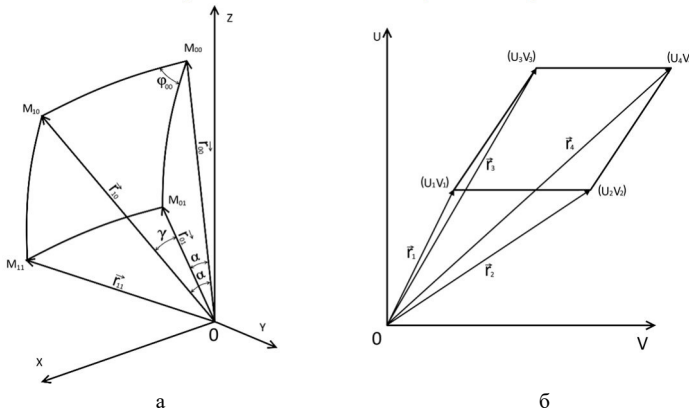


Fig. 3. Cell of fabric on the surface: a - spheres; b - cone depicted in cylindrical coordinates

$$X_i = r_i \cos \beta_i; \quad Y_i = r_i \sin \beta_i; \quad Z_i = c - \gamma r_i \quad (6)$$

β_i - rotation of the i -th vector projections from the OX axis;

$$C = \frac{1}{z_0}; \quad \gamma = \frac{c - z_0}{\sqrt{R_{\text{ш}}^2 - z_0^2}}$$

The corresponding equation of the unfolding of the cone in the plane with coordinates $U; V$ will be

$$U_1 = \gamma_1 r_i \cos \beta_i / \gamma_1 V_1 = \gamma_1 r_i \sin \beta_i / \gamma_1 \quad \text{Where } \gamma_1 = \sqrt{1 + \gamma^2} \quad (7)$$

We translate in the plane according to the above formulas (6; 7) arbitrary points 1, 2, 3 that are on the cone (Fig. 3 b) be:

$$r_i = \sqrt{X_i^2 + Y_i^2} \quad \beta_i = \arctg \frac{Y_i}{X_i}$$

The coordinates of the corresponding points on the plane will be

$$U_i = \frac{\gamma_i r_i \cos \beta_i}{\gamma_1} \quad V_i = \gamma_i r_i \sin \beta_i / \gamma_1$$

Figure 1 - it follows $\vec{r}_4 = \vec{r}_2 + \vec{r}_3 - \vec{r}_1$

$$r_4 = \frac{\sqrt{U_4^2 + V_4^2}}{\gamma_1} \quad \beta_4 = \frac{\arctg \frac{V_4}{U_4}}{\gamma_1}$$

$$X_4 = r_4 \cos \beta_4; \quad Y_4 = r_4 \sin \beta_4; \quad Z_4 = c - \gamma r_4$$

Thus, the coordinates of the knot points of the fabric can be determined using the formulas presented, sequentially changing the numbers of the points ($i = j = 1 \div N$) to the edge of the product, since the coordinates of the initial points will always be known.

Thus, as a result of theoretical studies, an analytical method has been developed for obtaining a scan of a tissue shell of a spatial shape.

In the case of insufficient forming ability of materials, it is required to analytically determine the geometric dimensions and location of the cutouts, which allow obtaining a volumetric shape, taking into account the forming properties of the material without deforming the sides of the cells.

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